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# Sliding mode control for a shunt active filtering

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*Abstract*—In this paper, the authors present a new control strategy using the sliding mode of the multicell converters which allows the compensation of the current harmonics in medium voltage networks. The use of these converters in the applications of active filtering is interesting since these converters allow to increase the bandwidth of the system while reducing the constraints on the components semiconductors.

*Keywords*— active filter, multicell converter, sliding mode control.

**Topic: T1 - Power electronics - converter control techniques.**

## I. INTRODUCTION

The introduction of multicell converters in power electronics systems opened new horizons in electrical engineering. This structure reduces the constraints on the semiconductors and reduces the share of reactive components. When a multicell converter with  $p$  cell is controlled using the same duty cycle on every cell and with a phase shift of  $\frac{2\pi}{p}$  between adjoining cells the ripple frequency of the output is  $pf_d$ . Another interesting feature of this converter is the self balancing of the flying capacitors voltages [1].

In our case we focus our study on the compensation of the current harmonics in a low voltage network using shunt active filtering with a sliding mode control. Figure 1 illustrates the principle of compensation. The shunt active filter should inject the current harmonics demanded by the load so that in the network is a pure sine wave.

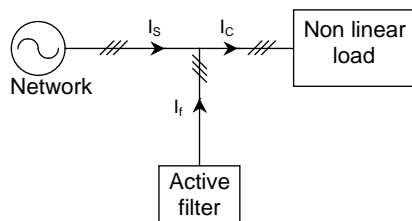


Fig. 1. Principle of shunt active filtering

## II. THE SLIDING MODE CONTROL

### A. Principle

The sliding mode control consists to force the trajectory of evolution of the state variables to converge towards a surface referred to as the "sliding surface". On this surface the order of the system is reduced and the trajectory of the variables of state slips up to the point of balance (fig. 4).

### B. Design of the control law

The control strategy presented here is given by using the instantaneous model of the system. It is based on the principle of stability of LYAPUNOV.

Taking the case of a  $p$  cell chopper. The state equation of the system is  $\dot{x} = Ax + G(x)u$ . It is noted that the system is non-linear. The scalar function  $V(x) = \frac{1}{2}\Delta x^T Q \Delta x$  is defined positively, its derivative is  $\dot{V}(x) = \Delta x^T Q \Delta \dot{x}$ .  $V$  represents the energy required to reach the point of balance. The stability criterion is given by the inequality (1) [2].

$$\Delta x^T Q G(x) \Delta u < 0 \quad (1)$$

with :  $u = U_{eq} + \Delta u$

$U_{eq}$  : equivalent control vectors ;

$\Delta u$  : relates the saturation of the control;

$Q$  : diagonal matrix containing reactive elements.

The  $p$  switching functions are defined to reach the point of balance asymptotically stable and verifying (1). They are given by (2).

$$s_i(x) = -\Delta x^T Q G(x) \quad (2)$$

In the case of a three-cell chopper (fig. 2), the instantaneous model of the system is given by (3).

$$\underbrace{\begin{pmatrix} \dot{i}_l \\ \dot{v}_{C1} \\ \dot{v}_{C2} \end{pmatrix}}_{\dot{\mathbf{x}}} = \underbrace{\begin{pmatrix} -\frac{R}{L} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}}_{\mathbf{A}} \underbrace{\begin{pmatrix} i_l \\ v_{C1} \\ v_{C2} \end{pmatrix}}_{\mathbf{x}} + \underbrace{\begin{pmatrix} \frac{v_{C1}}{L} & \frac{v_{C2} - v_{C1}}{L} & \frac{E - v_{C2}}{L} \\ -\frac{i_l}{C_1} & \frac{i_l}{C_1} & 0 \\ 0 & -\frac{i_l}{C_2} & \frac{i_l}{C_2} \end{pmatrix}}_{\mathbf{G}(\mathbf{x})} \underbrace{\begin{pmatrix} u_1 \\ u_2 \\ u_3 \end{pmatrix}}_{\mathbf{U}} \quad (3)$$

The switching functions obtained with a three-cell converter are given by (4).

$$s_i : \begin{cases} s_1 = 3i_{ref} \frac{v_{C1}}{E} - i_l \\ s_2 = 3i_{ref} \frac{v_{C2} - v_{C1}}{E} - i_l \\ s_3 = 3i_{ref} \frac{E - v_{C2}}{E} - i_l \end{cases} \quad (4)$$

To establish these switching functions, the control  $\delta u_i$  has to be positive when  $s_i$  is positive. To limit the switching frequency, a hysteresis function is introduced with a width of  $2\epsilon$ .

$$u_i : \begin{cases} 1 & s_i > \epsilon \\ 0 & s_i < -\epsilon \end{cases} \quad (5)$$

The figure (4) represents the three sliding surfaces and the evolution of the state variables in the plan  $(v_{c1}, v_{c2}, i_l)$ . There are three operating modes, the reaching mode ( $A \rightarrow B$ ), the sliding on a surface ( $B \rightarrow C$ ) where the state variables are reduced to 2 and finally the sliding on a line to reach the point of balance ( $C \rightarrow D$ ).

In order to operate with fixed frequency, a modulator is inserted. The connection between the switching functions

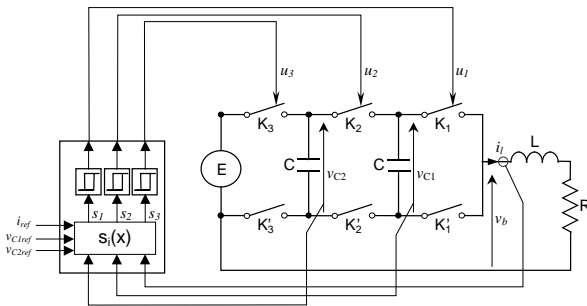


Fig. 2. Three-cell chopper with a sliding mode control at variable frequency

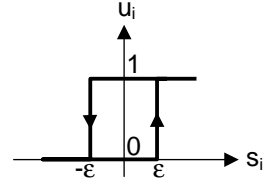


Fig. 3. function hysteresis function to limit the switching frequency

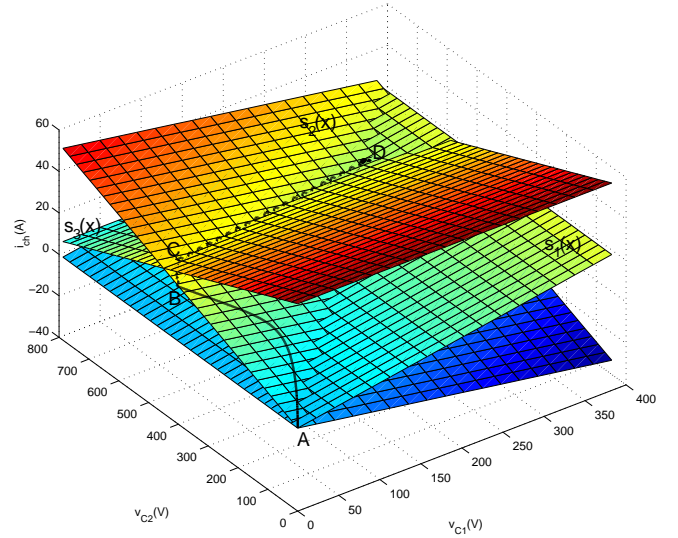


Fig. 4. Evolution of the state variables following the surfaces of slide for three cells chopper

and this modulator is done with a *PI* regulator and a filter (fig. 5).

The simulation results are represented on the figure (6). The amplitude current reference is  $20A$  and a frequency of  $1kHz$ . The load current follows correctly the current reference by ensuring a self balancing of flying capacitors voltages. We can note the existence of a certain shift phase in an operation at fixed switching frequency due to the modulator. Indeed the expression of phase shift between the input and the output for a *PWM* control signal is given by the equation (6) [4].

$$\Delta\phi = \frac{\pi f_m}{2 f_d} \quad (6)$$

$f_m$ : frequency of the signal of input.

$f_d$ : switching frequency.

Measured shift phase is of  $6.50^\circ$  degree, that given by the expression (6) is of  $5.62^\circ$  degree.

### III. SLIDING MODE CONTROL IN THREE-PHASE CURRENT

In the case of three-phase inverters, two structures of control are developed: interactive control and non-interactive control. The no-interactive control presents good dynamics performances compared to the interactive control.

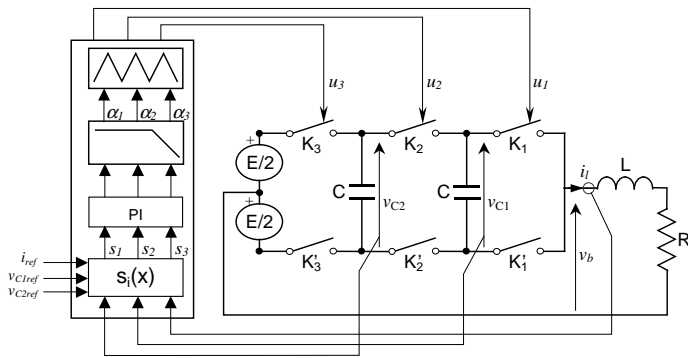


Fig. 5. Three-cell converter with the sliding mode control with fixed frequency

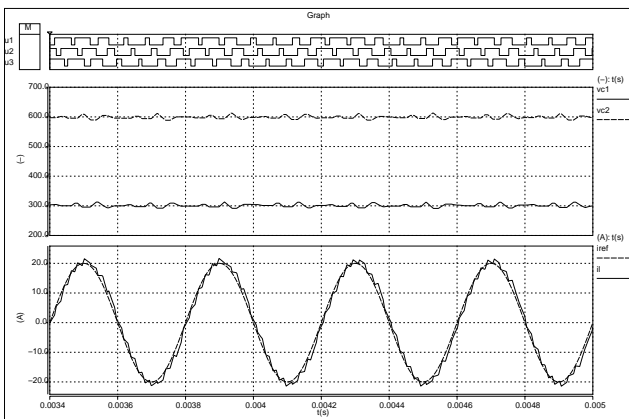


Fig. 6. Simulation at fixed frequency with a reference of 20A and 1kHz

The no-interactiv control consists to insert three legs side by side for make the three-phase inverter. The ordering of three legs is identical, the same control block described for the single phase inverter is used. This control strategy does not take account of the interaction between the legs.

#### A. Variable frequency control

Each control block is made of three "block of hysteresis" to obtain the control law. A simulation with a current reference of 20A and a frequency of 4.5kHz is represented by the figure (8). The average frequency of commutations of the switches is equal to the one of the current reference and is equal to the bandwidth of this control law. The converter has reached its dynamic limit which depends on the characteristics of the load. The self balancing of the flying capacitors voltage is always assured.

If the frequency of the reference exceeds the desired bandwidth the control is saturated, and commutations of the switches are done at a same time giving a two-level output voltage waveform.

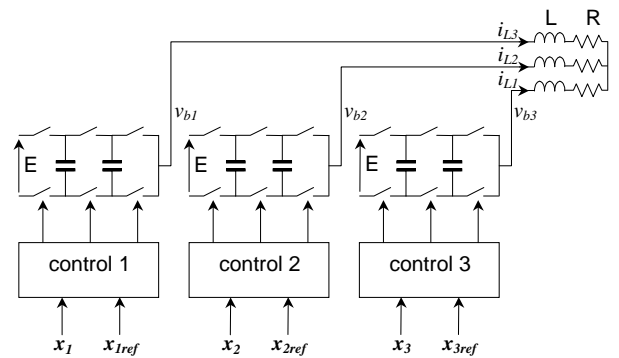


Fig. 7. No-interactiv sliding mode control

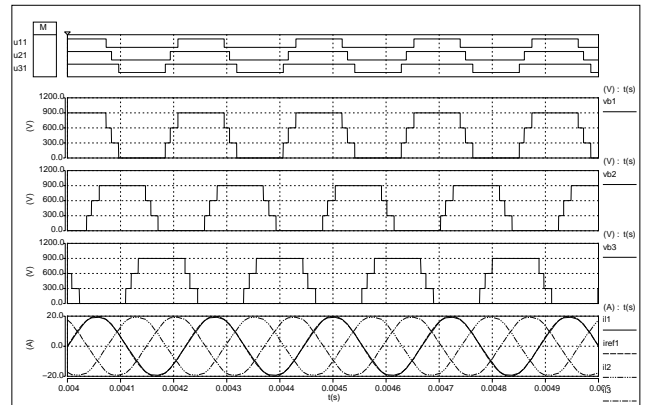


Fig. 8. Current and voltage for variable frequency control with  $I_m = 20A$  and  $f_m = 4.5kHz$

#### B. Fixed frequency control

Operation at fixed frequency in a three-phase inverter degrades considerably the phase-shift between the real and the desired currents in the load. Indeed for a current reference of 4.5kHz there is a phase-shift of 16.2° in simulation, with an attenuation of 10%. The switching frequency is equal to ( $f_d = 16kHz$ ). The Figure (10) represents the currents for an operation at fixed switching frequency.

### IV. ACTIVE FILTERING ON NETWORK LOW TENSION

The control system of the active filter is composed of two parts, the calculation of the harmonic currents and the generation of the control signals for the inverter using the sliding mode control.

#### A. Calculation of the harmonic currents

There are several algorithms for the extraction of the current harmonics. The method generally used is the method of the power  $pq$ . It allows to establish the components  $i_{ref\alpha}$  and  $i_{ref\beta}$  either for compensations of harmonics or for a compensation reactive power [5].

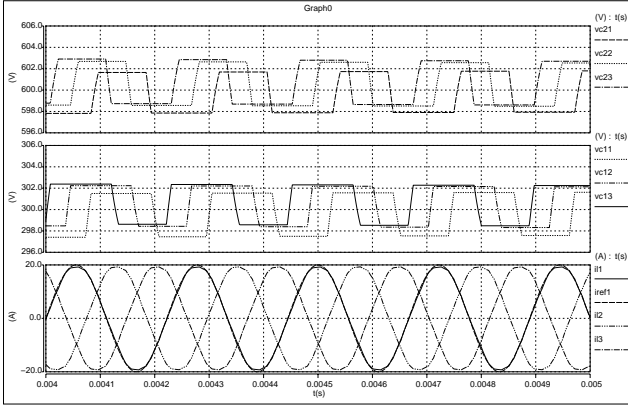
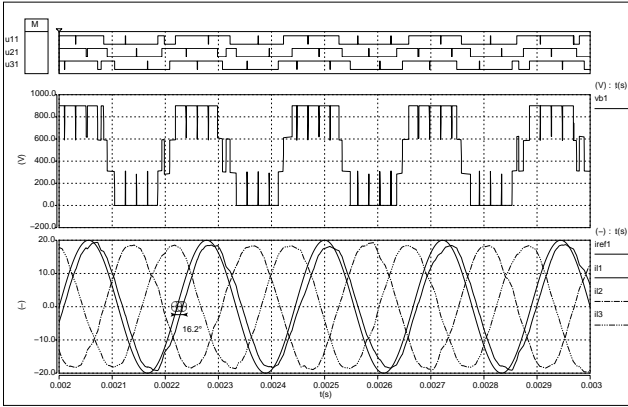


Fig. 9. Voltage balancing of the three legs

Fig. 10. Fixed frequency control with  $I_m = 20A$  and  $f_m = 4.5kHz$ 

$$\begin{pmatrix} p \\ q \end{pmatrix} = \begin{pmatrix} v_{s\alpha} & v_{s\beta} \\ -v_{s\beta} & v_{s\alpha} \end{pmatrix} \begin{pmatrix} i_{c\alpha} \\ i_{c\beta} \end{pmatrix} \quad (7)$$

$$\begin{pmatrix} i_{ref\alpha} \\ i_{ref\beta} \end{pmatrix} = \frac{1}{v_{s\alpha}^2 + v_{s\beta}^2} \begin{pmatrix} v_{s\alpha} & -v_{s\beta} \\ -v_{s\beta} & v_{s\alpha} \end{pmatrix} \begin{pmatrix} p_{ref} \\ q_{ref} \end{pmatrix} \quad (8)$$

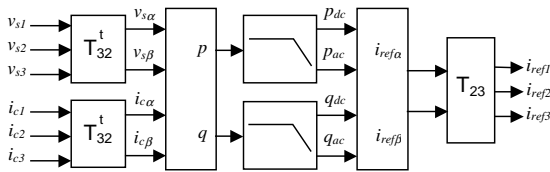


Fig. 11. General scheme for reference current identification

For a current harmonics compensation and to have a regulation of the DC capacitor voltage, we must impose  $p_{ref} = p_{ac} - p_{Cdc}$  and  $q_{ref} = q_{ac}$ .

$p_{Cdc}$  corresponds to the losses in the active filter.

## V. RESULTS OF SIMULATION

The results of simulation are obtained for a low voltage network of 220V. A bridge rectifier is regarded as the pol-

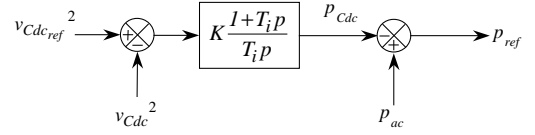


Fig. 12. scheme of DC voltage regulation

luting load as seen on figure (15), it absorbs a power of 6kW.

Network	$V_s$	220V
	$L_s$	650μH
Active filter	$C_{dc}$	100μF
	$L_f$	350μH
Load	$R_{ch}$	20Ω
	$L_{ch}$	1mH
	$L_c$	350μH

Fig. 13. Parameters of the shunt active filter, network and load

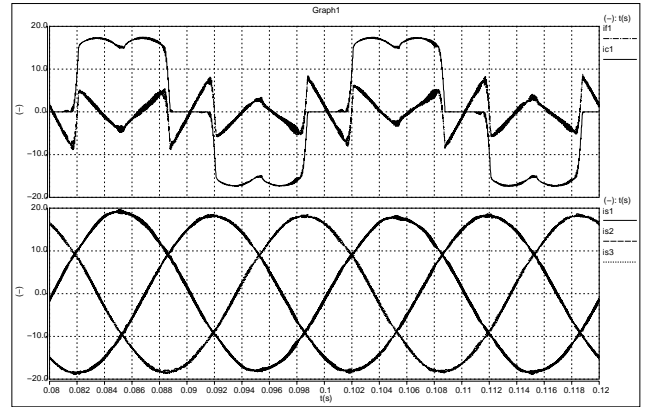


Fig. 14. a)-Load current and harmonic current of the first phase, b)-source currents

The comparisons are made under the same operating conditions. The THD is decreased from 25.97% without active filter to 2.23% with active filter using sliding mode control (Fig. 16 and 17).

## VI. CONCLUSIONS

The multicell converters by its dynamic performances makes it possible to cancel harmonics of high row and to obtain good performances. The sliding mode control at fixed frequency has a good bandwidth and it makes it possible to have a good compensation of current harmonics.

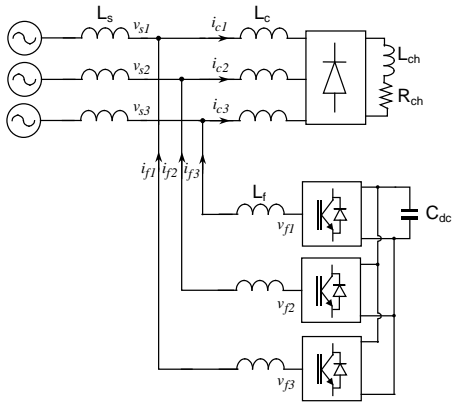


Fig. 15. Principale scheme of shunt active filter

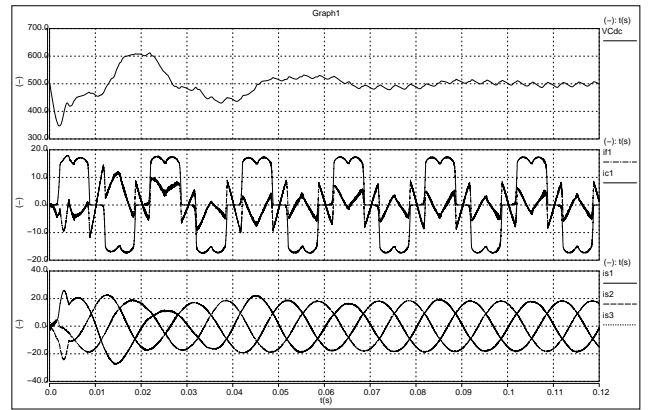


Fig. 18. Regulation of DC voltage

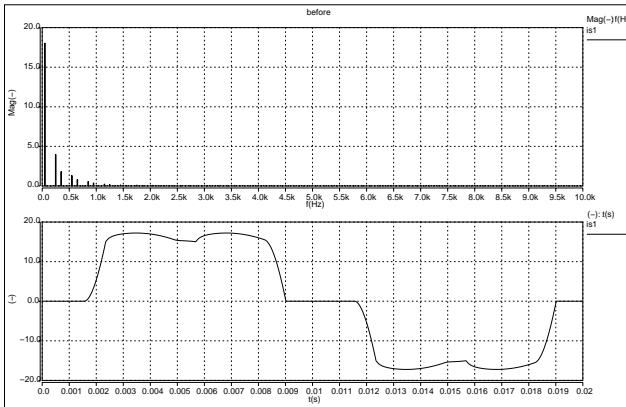


Fig. 16. Source current and spectrum waves before filtering

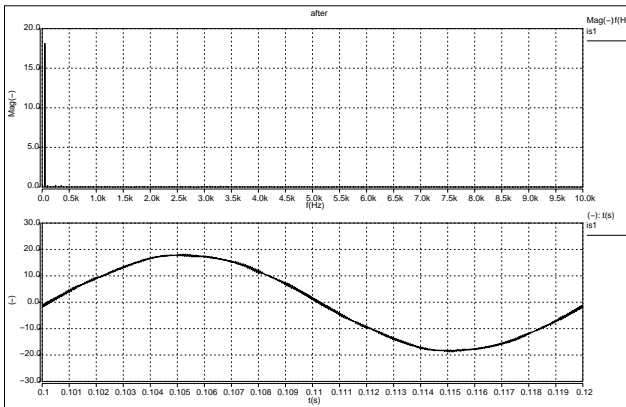


Fig. 17. Source current and spectrum waves after filtering

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